

### Appendix 3. The principle of Ordered Probit Regression

Due to our dependent variable is a discrete variable in order, and its distribution does not meet the requirements of the OLS model. Therefore, we use ordered probit regression to estimate the coefficient  $\beta_1$  and thus the total effect.

Assuming  $y^* = \mathbf{x}'\boldsymbol{\beta} + \varepsilon$  ( $y^*$  is an unobservable variable), the selection rule is given by:

$$y = \begin{cases} 0, & y^* \leq r_0 \\ 1, & r_0 \leq y^* \leq r_1 \\ 2, & r_1 \leq y^* \leq r_2 \\ \dots\dots\dots \\ J, & r_{J-1} \leq y^* \end{cases}$$

where  $r_0 < r_1 < r_2 < \dots < r_{J-1}$  are the parameters to be estimated, and are called "cutoff points".

Assuming  $\varepsilon \sim N(0,1)$  (normalize the variance of the perturbation term  $\varepsilon$  to 1), we have:

$$\begin{aligned} P(y = 0 | x) &= P(y^* \leq r_0 | x) = P(\mathbf{x}'\boldsymbol{\beta} + \varepsilon \leq r_0 | x) \\ &= P(\varepsilon \leq r_0 - \mathbf{x}'\boldsymbol{\beta} | x) = \Phi(r_0 - \mathbf{x}'\boldsymbol{\beta}) \\ P(y = 1 | x) &= P(r_0 \leq y^* \leq r_1 | x) = P(y^* \leq r_1 | x) - P(y^* < r_0 | x) \\ &= P(\mathbf{x}'\boldsymbol{\beta} + \varepsilon \leq r_1 | x) - \Phi(r_0 - \mathbf{x}'\boldsymbol{\beta}) \\ &= P(\varepsilon \leq r_1 - \mathbf{x}'\boldsymbol{\beta} | x) - \Phi(r_0 - \mathbf{x}'\boldsymbol{\beta}) \\ &= \Phi(r_1 - \mathbf{x}'\boldsymbol{\beta}) - \Phi(r_0 - \mathbf{x}'\boldsymbol{\beta}) \\ P(y = 2 | x) &= \Phi(r_2 - \mathbf{x}'\boldsymbol{\beta}) - \Phi(r_1 - \mathbf{x}'\boldsymbol{\beta}) \\ &\dots\dots\dots \\ P(y = J | x) &= 1 - \Phi(r_{J-1} - \mathbf{x}'\boldsymbol{\beta}) \end{aligned}$$

In this way, the sample likelihood function is obtained to further obtain the MLE estimator, i.e. the ordered probit model.